Efficiency Wage Models

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1 Motivation

Why is there unemployment? If a worker is willing to take a lower wage than the prevailing rate in the market, but she cannot find the job, it implies that there is a certain mechanism that prevents firms from lowering the wage. Efficiency Wage is one of such kinds of theories that rationalize this phenomenon. There are different considerations behind the notion of efficiency wage. For instance, paying a higher-than-market wage incentivizes workers to exert the desirable level of effort which is not directly observable by firms. Here efficiency wage plays an incentive role. Or ex-ante, under asymmetric information of employee's quality, a higher wage attracts more productive workers to apply for the job. Here, an efficiency wage arises as a screen device. Besides, the efficiency wage helps keep worker's morale and build loyalty. There is no single model that models all of these factors. Which factor matters the most depends on the specific contexts of the question.

2 A Generic Model

In the simplest case, the worker's effort is a function of wage $e(W)$, and the production is determined by efficiency unit $F(eL)$.

The firm maximizes profits by simultaneously choosing labor demand and wages.

$$Max_{\{L,w\}} \quad F(e(w)L) - wL$$

First-order conditions with respect to w and L are as below

$$F'(e(w)L)e'(w) = 1$$

$$F'(e(w)L)e(w) = w$$

Combining the two gives

$$\frac{e^w w}{e(w)} \equiv \epsilon_{e,w} = 1$$

This is a condition that is common across many efficiency wage models. It says the elasticity of effort with respect to wage should be equal to 1, namely both effort and wage change proportionally. It guarantees that in optimal the ratio of the two w/e, the unit cost of effective labor, is a constant.

Notice now wage is independently determined from labor supply. If total optimal labor demand $NL^* < L$, there is unemployment in equilibrium. Otherwise, the wage is bided up to clear the market.

3 An Extended Model

The effort may not only depend on wages paid to herself. How other jobs in the market are paid and the labor market condition as measured by the unemployment rate may also affect the effort level. Here we study such a model(Summers(1988)).

$$e(w,x) = \begin{cases} (\frac{w-x}{x})^{\beta} & \text{if } w > x \\ 0 & \text{otherwise} \end{cases}$$

where x is an indicator of the labor market condition defined as a function of the unemployment rate and market wage. b is a model parameter that captures the intensity of the effect of the unemployment rate.

$$x = (1 - bu)w_a$$

Regularity assumptions require $b > \beta$.

Taking the derivative of effort with respect to w, we get

$$e^w = \beta(\frac{w-x}{x})^{\beta-1}\frac{1}{x}$$

We know the optimal condition requires $\epsilon_{e,w} = 1$, that is

$$\epsilon_{e,w} = e^w w/e = \beta\frac{w}{\frac{w-x}{x}}\frac{1}{x} = 1$$

$$\beta w = w - x$$

$$(1-\beta)w = x$$

$$w = \frac{x}{(1-\beta)}$$

In the same time, equilibrium condition requires $w = w_a$, that is every firm needs to pay as equal as the market wage, which gives the following solution

$$u = \frac{\beta}{b} \equiv u_{EQ}$$

Notice now the unemployment rate only depends on parameters of effort function and does not depend upon production function. This is consistent with the fact that the unemployment rate does not have a trend.

We can also use numerical examples to show that w responds little to the labor market conditions, in particular u. The idea is that the cost-saving is very limited from lowering wages in response to an increase in unemployment. Here the cost is measured by cost per unit of effort. This is in line with the fact that firms do not adjust wages in response to short-run fluctuations.

4 Shapiro & Stiglitz(1984)

A micro-founded model of efficiency wage needs to specify the underlying mechanisms. e.g. the moral hazard problem introduced by imperfect monitoring of effort level by employers.

A firm and a worker. The worker chooses effort to be 0 or $\bar{e} > 0$, a discrete choice. The firm cannot monitor it directly, therefore, the wage cannot be based on the effort level. What the firm can do is to pay a wage that is incentive-compatible so that the worker does not shirk.

A worker has a reservation wage, which in the simplest case is assumed to be zero. The effort is costly, so she prefers shirking if there is no punishment. The penalty comes through a monitoring shock with a probability of q. Once found shirking, she gets fired. Besides, there is an exogenous breaking rate of the job b. The probability of finding a job is a. All are a Poisson process. Thus memoryless, namely the probability of entering a different state does not depend on the duration in the current state. It also allows us to work with the value function at any point in time by solely focusing on the state.

In summary, a worker is faced with three states: U(unemployed), E(Employed and not shirk) and S(employed and shirking).

The value of each state can be thought of as the PDV of an asset that pays dividends in each period subject to potential capital gains or losses if moving to a different state.

$$\rho V_U = a(V_E - V_U)$$

$$\rho V_S = w(bq)(V_U - V_S)$$

$$\rho V_E = (w - \bar{e})b(V_U - V_E)$$

Three equations above can be solved.

The incentive compatibility condition requires $V_S \leq V_E$, namely the worker cannot find it better to shirk than non-shirking.

In steady-state, we can also utilize the flow identity to pin down the relationship between a and b. It says the inflow and outflow of the employed population are equal to each other.

$$(1-u)b = ua$$

All together it gives the non-shirking condition (NSC), the centerpiece of the model.

$$w = \bar{e} + (\rho + \frac{b}{u})\frac{\bar{e}}{q}$$

Wage is now inversely correlated with the unemployment rate. This gives an upward sloping curve with wage and employment. The higher the unemployment rate, the more discipline it imposes to workers in a job from shirking as it is more painful to lose the job. As $u \to 0$, the wage needs to go positive infinity to incentivize the workers.

The term $\frac{\bar{e}}{q}$ can be thought of as an agency rent, which is commonly seen in such literature. Lower probability of detection and higher cost of effort implies higher rent from shirking.

Since the wage is determined by the NSC, the only free choice variable by the firm is the amount of labor to use. Labor demand is determined by the following condition

$$F(\bar{e}L)\bar{e} = w$$

It gives a downward sloping demand curve.

The intersection of NSC and labor demand pins down the equilibrium wage and employment. The unemployment rate is positive in equilibrium.

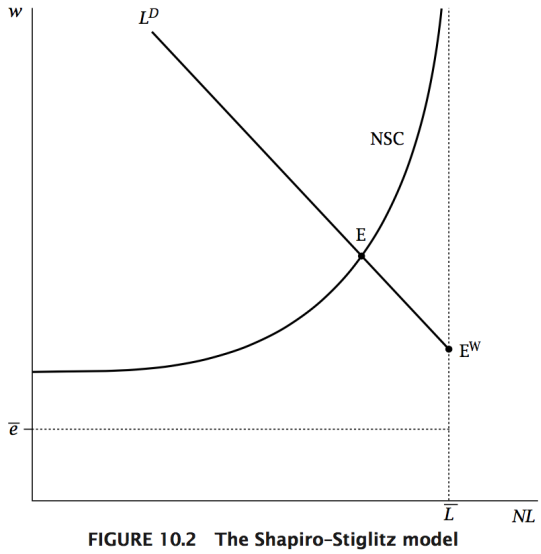

FIGURE 10.2 The Shapiro–Stiglitz model

Figure 1: Source: Romer's Textbook

What factors lead to a higher unemployment rate, thus a higher wage in equilibrium? Any factors that worsens the agency problom do so, i.e. lower chacen of detection q, higher effort cost, $\bar{e}$, higher job-breaking rate b.

One issue with the Shapiro & Stiglitz model is that It suggest the non-shirking condition curve is quite steep at a lower rate of unemployment. It implies wage is highly responsive to labor demand change, conflicting with the observed fact that wage adjusts little in response to labor demand.

The reason why this outcome is not efficient is simple. At full employment, the equilibrium is at E^W and marginal product of labor exceeds the cost of exerting effort $\bar{e}$. The government could bring the economy closer to more efficient allocation by subsidizing firms in a lum-sum manner to push up the labor demand curve. In the meantime, it should be noted that any unemployment insurance arrangement will worsen the problem because what it does is to push up the NSC further up. It alleviates the pain of losing a job.