# Economic Agents as Imperfect Problem Solvers - Ilut and Valchev (2023)

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#### Roadmap

#### Overview

The generic model

Application to consumption/saving

# Overview

Different types of behavioral models

 $\mathbb{E}(), u(), \rightarrow a$ 

- 1. Non-FIRE expectations: **𝔅** 
  - Incomplete information, Rational inattention, Learning, Extrapolation, Heterogeneous models
- 2. Non-standard preferences: *u*
- 3. Bounded rationality:  $\rightarrow$ 
  - Non-optimizing behaviors

## This paper

- Part 1: General framework
  - Dual-system reasoning [(Kahneman, 2011)]
  - Sometimes, deliberate optimization (system 2)
  - in other times, rule-of-thumb/heuristics (system 1)
  - Intuition: system 2 if state is sufficiently different from the past. system 1 if current state sufficiently resemble the previous state
- Part 2: application in consumption/saving (Aiyagari, 1994)
  - Consumers could get "stuck" in multiple system-1 regions
  - Implication: higher MPC than the standard model

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# The generic model

## Generic model

#### Standard problem

$$V\left(\overbrace{y_{t}}^{\text{state var}}\right) = \max_{c_{t} \in B(y_{t})} \left[u\left(y_{t}, c_{t}\right) + \beta \mathbb{E}_{t} V\left(y_{t+1}\right)\right]$$
$$y_{t+1} = F\left(y_{t}, c_{t}, v_{t+1}\right)$$
$$c^{*}: Y \to C$$

## Modeling dual-system reasoning

Assumption:  $c^*$  is costly to obtain, agents only observe noisy signals of it

$$\eta_t = c^*\left(y_t\right) + \underbrace{\sigma_{\eta,t}\varepsilon_t}_{\text{noises}}, \quad \varepsilon_t \sim N(0,1)$$

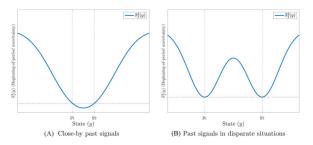
Additional assumption to make things tractable: non-parametric learning

$$c^*(y) = \sum_{j=1}^{\infty} \theta_j \underbrace{\phi_j(y)}_{\text{basis funcs}}$$

#### Automatic system 1

associative memory

$$\mathbb{E}\left(c^*(y) \mid \eta^{t-1}, y^{t-1}\right)$$





Associative Memory and System 1 Uncertainty at Time t = 3:  $\hat{\sigma}_2^2(y)$ 

Plotted based on two signals  $\eta_1$  and  $\eta_2$  with equal precision, at state realizations

#### Occasional deliberate system 2

costly reducing uncertainty about  $c^*(y)$ 

- Invoked only if prior uncertainty  $\hat{\sigma}_{t-1}^2(y_t)$  is high enough, exceeds a threshold  $\kappa$ 

$$\begin{split} \min_{c_t,\sigma_{\eta,t}^2} \mathbb{E} \left[ (c_t - c^* \left( y_t \right))^2 \mid \eta^t, y^t \right] + \underbrace{\operatorname{cost of deliberation}}_{\kappa} \underbrace{\operatorname{In} \left( \frac{\widehat{\sigma}_{t-1}^2 \left( y_t \right) + \sigma_{\eta,t}^2}{\sigma_{\eta,t}^2} \right)} \\ \to c_t = \widehat{c}_t(y_t), \quad \widehat{\sigma}_t^2 \left( y_t \right) = \min \left[ \kappa, \widehat{\sigma}_{t-1}^2 \left( y_t \right) \right] \\ \to \sigma_{\eta,t}^{*2} = \begin{cases} \frac{\kappa \widehat{\sigma}_{t-1}^2 \left( y_t \right)}{\widehat{\sigma}_{t-1}^2 \left( y_t \right) - \kappa}, & \text{if} \quad \widehat{\sigma}_{t-1}^2 \left( y_t \right) > \kappa, \\ \infty, & \text{if} \quad \widehat{\sigma}_{t-1}^2 \left( y_t \right) \leqslant \kappa. \end{cases} \end{split}$$

## Action rule from the dual-system

$$c_t = \widehat{c}_t \left( y_t \right) = \widehat{c}_{t-1} \left( y_t \right) + \alpha_t^* \left( y_t \right) \left( \eta_t - \widehat{c}_{t-1} \left( y_t \right) \right)$$
$$\alpha_t^* \left( y_t \right) \equiv \frac{\widehat{\sigma}_{t-1}^2 \left( y_t \right)}{\widehat{\sigma}_{t-1}^2 \left( y_t \right) + \sigma_{\eta,t}^{*2}} = \max \left[ 1 - \frac{\kappa}{\widehat{\sigma}_{t-1}^2 \left( y_t \right)}, 0 \right]$$

#### Implications:

- Agents follow default, habitual behavior in familiar situations, but rethink that behavior in novel situations.
- Agents may fall into a learning trap, namely habitual yet non-optimal behaviors when system 1 uncertainty is low enough, and the behaviors lead to self-fulfilling value of state variable.

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# Consumption/saving with costly deliberation

# Standard problem

[Aiyagari, 1994]

#### Model

$$V\left(\overbrace{y_{i,t}}^{\text{cash in hand}}\right) = \max_{c_{it}} u\left(c_{i,t}\right) + \beta \mathbb{E}_t V\left(y_{i,t+1}\right)$$
$$y_{i,t+1} = (1+r)\left(y_{i,t} - c_{i,t}\right) + ws_{i,t+1}$$
$$c_{i,t} \le y_{i,t}$$

## This paper

#### Costly deliberation friction

$$\eta_{i,t} = \overbrace{c^*(y_{i,t})}^{\text{optimal c func}} + \varepsilon_{i,t}, \quad \varepsilon_{i,t} \sim N\left(0, \sigma_{\eta,i,t}^2\right)$$
$$\widehat{\sigma}_{i,t}^2\left(y_{i,t}\right) = \min\left[\kappa, \widehat{\sigma}_{i,t-1}^2\left(y_{i,t}\right)\right]$$
$$\widehat{c}_{i,t}\left(y_{i,t}\right) = \widehat{c}_{i,t-1}\left(y_{i,t-1}\right) + \alpha_{i,t}\left(y_{i,t}\right)\left(\eta_{i,t} - \widehat{c}_{i,t-1}\left(y_{i,t-1}\right)\right)$$
$$c_{i,t} = \min\left(y_{i,t}, \widehat{c_{i,t}}\left(y_{i,t}\right)\right)$$

## Implications

There are two locally stable learning traps: high-confidence suboptimal consumption policies

1. HtM agents centered around borrowing constraints

Perfect foresight consumption policy

$$\bar{y}_i = w \text{ and } \hat{c}_i \left( \bar{y}_i \right) > \qquad \qquad \widehat{c^{RW} \left( \bar{y}_i \right)} \qquad \qquad = \bar{y}_i$$

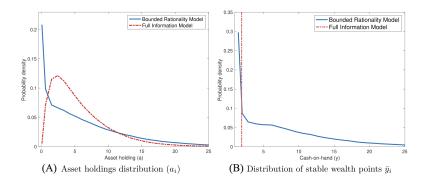
2. Away from borrowing constraint, yet with high MPCs, steeper than perfect-forecast consumption policy

$$\bar{y}_i > w \text{ and } \hat{c}_i(\bar{y}_i) = c^{RW}(\bar{y}_i) < \bar{y}_i, \frac{\partial \hat{c}_i}{\partial y}(\bar{y}_i) > \frac{\partial c^{RW}}{\partial y}(\bar{y})$$

#### Macro implications

Stationary wealth distribution

• High fraction of agents in learning traps (71%)



Aiyagari, S Rao (1994). "Uninsured idiosyncratic risk and aggregate saving". The Quarterly Journal of Economics 109.3, pp. 659–684.
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Kahneman, Daniel (2011). Thinking, fast and slow. macmillan.